Total Pages : 3

Roll No. .....

# **MSCPH-504**

## **Statistical Mechanics**

#### M.Sc. PHYSICS (MSCPH-21)

Ist Semester Examination, 2022 (June)

#### Time : 2 Hours]

#### Max. Marks : 80

**Note :** This paper is of Eighty (80) marks divided into two (02) Sections A and B. Attempt the questions contained in these sections according to the detailed instructions given therein.

### SECTION-A

# (Long Answer Type Questions)

**Note :** Section 'A' contains Five (05) long answer type questions of Twenty (20) marks each. Learners are required to answer any Two (02) questions only.

 $(2 \times 20 = 40)$ 

1. What is partition function? Obtain it for a monoatomic perfect gas represented by the canonical ensemble. Find expressions for free energy, entropy and internal energy of the gas in terms of its partition function.

#### C159/MSCPH-504

- 2. Show that a system of classical harmonic oscillators Helmholtz free energy is  $NkTln(\hbar\omega)/kT$ ) and also show its complete agreement with the equipartition theorem.
- **3.** Explain Bose-Einstein condensation. How does it differ from ordinary condensation? Derive the critical temperature at which this phenomenon sets in.
- 4. What are the phase transitions of first and second kind? Discuss Ising model for phase transitions of second kind.
- 5. (a) Show that the molar specific heat of a strongly degenerate boson gas is given as  $C_v = 1.92 \text{ R}(\text{T/T}_C)^{3/2}$ , Represent it graphically.
  - (b) Show that electron gas in a white Dwarf Star is strongly degenerate and relativistic in nature.

### SECTION-B

# (Short Answer Type Questions)

- **Note :** Section 'B' contains Eight (08) short answer type questions of Ten (10) marks each. Learners are required to answer any Four (04) questions only.  $(4 \times 10 = 40)$
- **1.** Explain the meaning of :
  - (a) Microstate.
  - (b) Macrostate.
  - (c) Ensemble in statistical mechanics.

C159/MSCPH-504 [2]

- 2. Consider a system of two particles each having only 3 quantum states of energy 0,  $\varepsilon$ ,  $2\varepsilon$  system is in contact with a heat reservoir at temperature T. Write down the partition function for the system obeys
  - (a) Fermi Dirac statistics.
  - (b) Bose Einstein statistics.
- **3.** Derive Sackur Tetrode equation for the entropy of an ideal monoatomic gas. How does it resolve the Gibb's Paradox?
- **4.** A system consisting of 3 independent particles localized in space. Each particle has two states of energy 0 and ε. When the system is in thermal equilibrium with a heat reservoir at temperature T, calculate its partition function?
- **5.** Compare the three statistics Bose- Einstein, Fermi-Dirac and Maxwell Boltzmann Statistics.
- 6. What do you mean by phase space? Using this concept find the number of phase cells for one dimensional simple harmonic oscillator.
- 7. Show that the mean speed of an electron in an electron gas at  $T = oK \ \overline{v} = \frac{3v_F}{4}$ , where  $v_F$  is the speed of an electron at the Fermi energy.
- **8.** Define phase transition? Distinguish between first and second order phase transitions with suitable examples.