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Total Pages : 4

Roll No.

MT-610

Mathematical Programming-II

MA/MSc Mathematics (MAMT/MScMT)

4th Semester Examination, 2022 (Dec.)

Time : 2 Hours]

[Max. Marks : 35

Note : This paper is of Thirty Five (35) marks divided into two (02) Sections A and B. Attempt the questions contained in these sections according to the detailed instructions given therein.

SECTION–A

(Long Answer Type Questions)

Note : Section 'A' contains Five (05) long answer type questions of Nine and Half ($9\frac{1}{2}$) marks each. Learners are required to answer any Two (02) questions only.

($2 \times 9\frac{1}{2} = 19$)

1. Solve the following NLPP using the Kuhn-Tucker conditions

$$\begin{aligned} \text{Maximize} \quad & z = 2x_1^2 - 7x_2^2 + 12x_1x_2 \\ \text{Subject to} \quad & 2x_1 + 5x_2 \leq 98, \\ & x_1 \geq 0, x_2 \geq 0. \end{aligned}$$

2. Use Beal's method to solve the following quadratic problem

$$\begin{aligned} \text{Maximize} \quad & z = 2x_1 + 3x_2 - x_1^2 \\ \text{Subject to} \quad & x_1 + 2x_2 \leq 4, \\ & x_1 \geq 0, x_2 \geq 0. \end{aligned}$$

3. Using Bellman's principle of optimality,

$$\begin{aligned} \text{Minimize} \quad & z = y_1^2 + y_2^2 + \dots + y_n^2 \\ \text{Subject to constraints} \quad & y_1 + y_2 + \dots + y_n = b, \\ & y_i \geq 0; i = 1, 2, \dots, n \end{aligned}$$

4. Solve the following LPP by dynamic programming

$$\begin{aligned} \text{Maximize} \quad & z = 2x_1 + 5x_2 \\ \text{Subject to constraints} \quad & 2x_1 + x_2 \leq 430, \\ & 2x_2 \leq 460, \\ & x_1 \geq 0, x_2 \geq 0. \end{aligned}$$

5. Discuss Convex Separable programming also write its algorithm.

SECTION-B

(Short Answer Type Questions)

Note : Section 'B' contains Eight (08) short answer type questions of Four (04) marks each. Learners are required to answer any Four (04) questions only. (4×4=16)

1. Give the characteristics of dynamic programming problems.
2. State Bellman's optimality principle.
3. Write recursive relations using dynamic programming to the problem

Maximize

$$z = x_1^2 + x_2^2 + x_3^2 + x_4^2$$

Subject to constraints

$$x_1 x_2 x_3 x_4 = 16$$

$$x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, x_4 \geq 0$$

4. Write four applications of dynamic programming problem.
5. Write a short note on duality in quadratic programming.
6. Give a general framework for constrained non linear programming problem.
7. Write algorithm for Beal's method to solve quadratic programming problem.

8. Define the following :

(a) Separable function.

(b) Convex programming problem.
